

# Initialization of FCME Algorithm for Noise Floor Estimation

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## 1 Introduction

In this paper, we investigate a real-time noise power estimation with Forward Consecutive Mean Excision (FCME) algorithm. In the real-time noise power estimation, the observed samples may include both noise-only samples ( $H_0$ ) and noise-plus-signal samples ( $H_1$ ) [1]. The FCME algorithm extracts noise-only samples with an iterative process in which a set of estimated noise-only samples is updated iteratively. We investigate an appropriate size for the initial noise samples set, denoted by  $|\mathbf{Q}_0|$ , in FCME algorithm while  $|\mathbf{Q}_0|$  is typically assumed to be 10% smallest samples from the total observed samples ( $N$ ). In this paper, the appropriate size  $|\mathbf{Q}_0|$  is obtained analytically based on a relationship between false alarm rate ( $P_{FA}$ ) and  $|\mathbf{Q}_0|$ .

## 2 Relationship between Noise Floor Estimation Performance and $|\mathbf{Q}_0|$

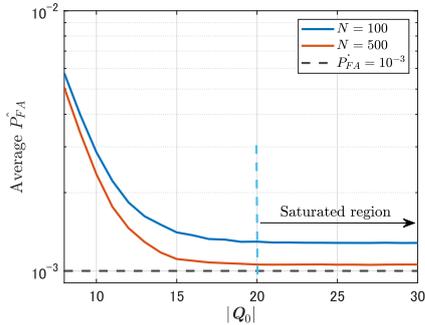


Fig. 1: Average  $\hat{P}_{FA}$  with  $|\mathbf{Q}_0|$  in noise-only case

Fig. 1 shows the average obtained false alarm rate  $\hat{P}_{FA}$  as a function of  $|\mathbf{Q}_0|$  with  $N = 100, 500$  and target false alarm rate  $P_{FA} = 10^{-3}$ . For both  $N$ , the average  $\hat{P}_{FA}$  become saturated in the region where  $|\mathbf{Q}_0| > 20$  and the gap between the average  $\hat{P}_{FA}$  and  $P_{FA}$  are relatively small. As an indication of the saturated region, we define appropriate  $|\mathbf{Q}_0|$  to be the minimum value of  $|\mathbf{Q}_0|$  within the saturated region.

## 3 Approximated Theoretical Average $P_{FA}$

The average  $P_{FA}$  in [2] is approximated by

$$\text{Average } P_{FA} \approx \sum_{i=|\mathbf{Q}_0|}^{|\mathbf{Q}_0|+5} (\alpha_{i-1} - \alpha_i)(\kappa_i) + \left(1 - \sum_{i=|\mathbf{Q}_0|}^{|\mathbf{Q}_0|+5} (\alpha_{i-1} - \alpha_i)\right) \frac{1}{(1 + T_{CME}/N)^N}. \quad (1)$$

where  $i$  is the index number of the sorted  $H_0$  samples,  $\alpha_i$  is the probability that  $(i+1)$ th  $H_0$  sample being

successfully collected into the assumed noise samples set and  $\kappa_i$  is the biased  $P_{FA}$  when only  $i$  samples out of  $N$  sorted samples are successfully collected [3]. Let the probability that FCME algorithm succeeds to collect samples up to  $i$  samples and finally stops at  $(i+1)$ th sample denoted as  $(\alpha_{i-1} - \alpha_i)$ , average  $\hat{P}_{FA}$  can be calculated based on the summation of multiplication between  $(\alpha_{i-1} - \alpha_i)$  and the corresponding  $\kappa_i$  from  $i = |\mathbf{Q}_0| \sim N$ . The appropriate  $|\mathbf{Q}_0|$  is obtained based on the relationship between Average  $\hat{P}_{FA}$  and  $|\mathbf{Q}_0|$ . Specifically, the minimum  $|\mathbf{Q}_0|$  in the saturated region like in Fig. 1 is chosen as the appropriate  $|\mathbf{Q}_0|$ .

## 4 Numerical Evaluation and Conclusion

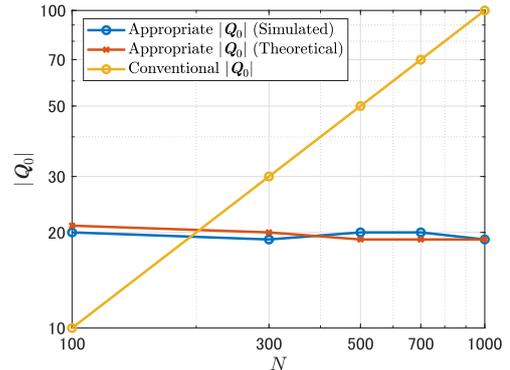


Fig. 2: Appropriate  $|\mathbf{Q}_0|$  vs  $N$

Fig. 2 shows selected  $|\mathbf{Q}_0|$  as a function of  $N$  by typical approach, i.e. 10% of  $N$ , the proposed appropriate  $|\mathbf{Q}_0|$ , and simulation result. Specifically, in the  $|\mathbf{Q}_0|$  with simulation result,  $|\mathbf{Q}_0|$  is chosen empirically from the simulation result in Fig. 1. It can be seen that the proposed appropriate  $|\mathbf{Q}_0|$  and simulation result remain relatively constant with  $N$  in contrast to the conventional approach which assumes that  $|\mathbf{Q}_0|$  is 10% of  $N$ .

## References

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